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Image: Ornamental multiplication of space-time figures of temperature transformation rules (adapted from T. S. Bíró and P. Ván 2010 EPL 89 30001; artistic impression by Frédérique Swist).
Creep motion of a domain wall in the two-dimensional random-field Ising model with a driving field

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Abstract – With Monte Carlo simulations, we study the creep motion of a domain wall in the two-dimensional random-field Ising model with a driving field. We observe the nonlinear field-velocity relation, and determine the creep exponent \( \mu \). To further investigate the universality class of the creep motion, we also measure the roughness exponent \( \zeta \) and energy barrier exponent \( \psi \) from the zero-field relaxation process. We find that all the exponents depend on the strength of disorder.

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Introduction. – In recent years the dynamics of elastic systems in disordered media has been the focus of theoretical and experimental studies. Examples are charge-density waves, vortex lattices, domain walls in ferromagnetic or ferroelectric materials, contact lines, and fluid invasion in porous media [1–6]. In particular, the magnetic domain-wall dynamics is an important topic in magnetic devices, nanomaterials, thin films, and semiconductors [7–10]. At zero temperature, the domain-wall motion exhibits a depinning transition. Due to the energy barriers created by the disorder, the domain wall is pinned and the velocity of the domain wall remains zero up to a critical field \( H_c \) [11–14]. At finite temperature, the depinning transition is softened and the energy barriers can always be overcome by thermal activation. Thus, with a sufficiently small field, \( H \ll H_c \), the domain-wall motion can reach a steady state, which is known as the creep motion [2,15–17].

Up to date, most theoretical approaches to the domain-wall dynamics in ferromagnetic materials are typically based on the Edwards-Wilkinson equation with quenched disorder (QEW). This equation is a phenomenological model, and detailed microscopic structures and interactions of real materials are not concerned. To further understand the domain-wall motion from a more fundamental viewpoint, we should build lattice models based on microscopic structures and interactions. The random-field Ising model with a driving field (DRFIM) is a candidate, at least to capture robust features of the domain-wall motion, although it does not include all interactions in real materials. It may go beyond the QEW equation, reveal new universality classes, explain a wider range of physical phenomena, and allow a closer comparison with experiments. For example, the depinning transition of the two-dimensional DRFIM model has been examined with the short-time dynamic approach [18–20]. The critical exponents are accurately determined, and the results indicate that the DRFIM model and QEW equation are not in the same universality class. In a very recent work, it is demonstrated that the relaxation state and relaxation-to-creep transition of the domain-wall motion can be simulated with the DRFIM model, and the Cole-Cole plot of the complex susceptibility obtained in the experiments is nicely reproduced [21,22].

The main purpose of this paper is to study the creep motion of the domain wall in the two-dimensional DRFIM model, in comparison with the QEW equation and experiments. In the creep regime of the domain-wall motion, the field-velocity relation is expected to be

\[ v \sim \exp[-(H_c/H)^\mu/T], \]

where \( \mu \) is the creep exponent, usually used to classify the universality class of the materials in experiments [2,5,23].

Based on the QEW equation, two universality classes have been identified for the field-induced domain-wall motion in two dimensions [17,24]: \( \mu = 1/4 \) belongs to the random-bond disorder, whereas \( \mu = 1 \) to the random-field
disorder, respectively. In the past years, most experiments confirmed this result. However, recent progress in experiments suggests that the degree of surface roughness may alter the universality class [25]. Different values of $\mu$ between 1 and 1/4 are also reported [26,27]. Due to the uncertainty of the domain-wall dimensionality, this leads to conflicts in identifying the universality classes of the materials [26,28]. These experimental results challenge our theoretical understanding. In the QEW equation, the strength of disorder is thought to be irrelevant to the universality class.

On the other hand, based on the QEW equation, one may theoretically derive the scaling law [29]

$$\mu = \frac{2\zeta + d - 2}{2 - \zeta},$$

(2)

where $\zeta$ is the equilibrium roughness exponent. In the numerical study of the QEW equation, however, a violation of the scaling law in eq. (2) is observed for low temperatures or with strong disorder [29], which implies a more complicated physical scenario. Moreover, it is argued in ref. [30] that instead of eq. (2), the creep exponent should obey the scaling law

$$\mu = \frac{\psi}{2 - \zeta},$$

(3)

where $\psi$ is the energy barrier exponent without a driving field [30,31]. The scaling laws in eqs. (2) and (3) will be equivalent if $\psi$ is identical to the ground-state–energy fluctuation exponent $\theta$,

$$\psi = \theta \equiv 2\zeta + d - 2.$$  

(4)

Theoretically, there are still some controversies on the value of $\psi$ [15,30,32].

In order to fully understand the creep motion and its universality class, it is important to directly determine the exponents $\psi$ and $\zeta$. This can be done by independently simulating the zero-field relaxation process of a domain wall [15,32]. Since the driving field is absent, the correlated domain-wall segment of a length $\xi$ overcomes the energy barrier $U(\xi)$ only by thermal activation. According to the Arrhenius law, the time scale of this activation process is the order of $\exp[U(\xi)/T]$. It is believed that the energy barrier may scale as $U(\xi) \sim \xi^\psi$ for a large $\xi$. Therefore, at long times, the correlation length should grow by a logarithmic law,

$$\xi(t) \sim [T \ln(t/t_0)]^{1/\psi}.$$  

(5)

As the domain wall propagates, it continues to roughen as an interface. The roughness function of the domain interface is believed to scale as [14,18,33–35]

$$\omega^2(t) \sim \xi(t)^{2\zeta},$$

(6)

where $\zeta$ is the equilibrium roughness exponent.

Early numerical study of the DRFIM model also intended to tackle the creep motion [16]. However, due to the limited range of the driving fields, the validity of eq. (1) is not conclusively confirmed. Further understanding of the scaling laws in eqs. (3) and (4) is also lacking. In particular and more importantly, in this paper, we investigate the possible dependence of the universality class on the strength of the disorder.

The model. – The two-dimensional DRFIM model is defined by the Hamiltonian

$$\mathcal{H} = -J \sum_{<ij>} S_i S_j - \sum_i (h_i + H) S_i,$$

(7)

where $S_i = \pm 1$ is an Ising spin on the square lattice. The quenched random field $h_i$ is uniformly distributed within an interval $[-\Delta, \Delta]$, and $H$ is a homogeneous driving field.

In this paper, we take the coupling constant $J = 1$. Since the two-dimensional random-field Ising model does not have a long-range ordered phase, one expects that domains grow spontaneously in the bulk at a finite temperature. This may lead to ambiguity in defining a single domain interface. If it is at low enough temperatures, however, the dynamic evolution of the bulk is negligible. In our study, the temperature is restricted to $T_{\text{max}} = 0.67$.

Our simulations are performed on a lattice, with a linear size $2L$ in the $x$-direction and $L$ in the $y$-direction. Antiperiodic and periodic boundary conditions are adopted in the $x$ and $y$ directions, respectively. To eliminate the pinning effect irrelevant for the quenched disorder, we rotate the square lattice such that the initial domain wall orients in the (11) direction of the square lattice, as shown in refs. [11,16,18,36].

The initial state is a semiordered state with a perfect domain wall in the $y$-direction. After preparing the initial state, we randomly select a spin, and flip it with the heat-bath algorithm. A Monte Carlo time step is defined by $2L^2$ single-spin flips. Simulations are performed at two temperatures $T = 0.33$ and 0.67 with lattice size $L = 256$ up to $t_{\text{max}} = 10^6$. For the strength of random fields, five typical values of $\Delta$ are chosen, i.e., $\Delta = 0.5, 0.7, 1.0, 1.2$ and 1.5. For $\Delta = 1.5$, the bulk may also evolve. Therefore, we update only those spins at the domain interface, i.e., a spin will be flipped only if at least one of the nearest neighbors is already flipped [37,38]. Simulations of different $L$ are also performed to confirm that the finite-size effects are already negligibly small. For the simulations of the creep motion, the domain-wall velocity is averaged by at least 1000 samples. For the zero-field relaxation process, the total samples are 5000. Errors are estimated by dividing the samples into three or four subgroups.

To study the creep motion and zero-field relaxation of the domain interface, we first introduce a line magnetization

$$m(y, t) = \frac{1}{L} \sum_{x=1}^L S_{xy}(t).$$

(8)
Here $S_{xy}(t)$ denotes a spin at site $(x, y)$. The height function of the interface is defined as

$$h(y, t) = \frac{L}{2}[m(y, t) + 1].$$

With the height function at hand, the average velocity of the interface can be calculated

$$v(t) = \left\langle \frac{dh(y, t)}{dt} \right\rangle,$$

where $\langle \cdots \rangle$ includes the statistical average and average over $y$.

With the height function $h(y, t)$, the roughness function of the interface is defined as

$$\omega^2(t) = \langle(h(y, t)^2) - \langle h(y, t) \rangle^2 \rangle.$$

A more informative quantity is the height correlation function [34],

$$C(r, t) = \langle[h(y + r, t) - h(y, t)^2] \rangle.$$

It describes both the spatial correlation of the height function in the $y$-direction and the growth of the domain interface in the $x$-direction.

For a sufficiently large lattice, i.e., the correlation length $\xi(t) \ll L$, we should observe the standard scaling behavior for the roughness function in eq. (6), and that for the height correlation function [14, 18, 33–35],

$$C(r, t) = 2\omega^2(t) f(r/\xi).$$

**Monte Carlo simulations.** – To investigate the characteristic relation between the driving field $H$ and domain-wall velocity $v$, we measure the velocity for a given driving field when the steady state is reached. Theoretically the creep regime is expected to be far below the critical point $H_c$. For a smaller driving field $H$, however, it takes a longer time to reach the steady state. In our simulations, the longest time is $10^6$ Monte Carlo time steps.

In fig. 1, we plot the velocity $v$ as a function of $(H_c/H)^{\psi}/T$. By adjusting the exponent $\mu$, one may observe a linear curve. Thus the nonlinear field-velocity relation in eq. (1) is verified in the two-dimensional DRFIM model. For $\Delta = 1.2$, we obtain $\mu = 1.02(5)$ and 0.95(8) at $T = 0.67$ and 0.33, respectively, close to the theoretical prediction $\mu = 1$ based on the QEW equation. The small deviation from the exponential law for large fields suggests that the domain-wall motion leaves the creep regime. For $\Delta = 0.5$, however, the fitted exponent is $\mu = 0.63(5)$ and 0.59(4) at $T = 0.67$ and 0.33, respectively, significantly smaller than the theoretical value $\mu = 1$ of the QEW equation. For $\Delta = 1.5$, the dynamic evolution becomes very slow at lower temperatures, and we are able to obtain results only at $T = 0.67$. The exponent $\mu = 1.14(5)$ differs also from that of the QEW equation. To further confirm our results, we may plot $\ln v$ against $H_c/H$ on a log-log scale. From slopes of the curves, we measure the exponent $\mu$. Or, we may directly fit the numerical data to the formula in eq. (1) to extract $\mu$. All these techniques yield similar values for the exponent $\mu$.

In ref. [16], it is stated that the numerical data could fit to the field-velocity relation in eq. (1) in the limit $\mu \to 0$. In the inset of fig. 1, we plot $v$ against $\ln(H_c/H)/T$ for $\Delta = 1.2$ and $T = 0.67$ on a semi-log scale. A tendency of a linear behavior is observed for large driving fields, supporting the results in ref. [16]. Therefore we believe that the field regime considered in ref. [16] is too large to observe the creep motion.

To verify the scaling laws in eqs. (3) and (4), one needs to determine the exponents $\psi$ and $\zeta$ independently. Thus we simulate the zero-field relaxation process of the domain wall. In the absence of the driving field $H$, the growth law of the correlation length $\xi(t)$ plays a crucial role. To extract the correlation length $\xi(t)$, we use a data collapse technique based on the scaling behavior of the height correlation function. According to eq. (13), we fix $t' = 10^6$, and rescale $r$ of another $t$ to $\xi(t')/\xi(t) r$ and $C(r, t)$ to $\omega^2(t')/\omega^2(t) C(r, t)$. If the ratio of $\xi(t')/\xi(t)$ is properly chosen, $C(r, t)$ at different time $t$ collapse onto a single curve. This is shown for $\Delta = 1.2$ and $T = 0.67$ in the inset of fig. 2. In other words, one may estimate the ratio $\xi(t')/\xi(t)$ from the data collapse of $C(r, t)$. Thus, up to a constant $\xi(t_0)$, the growth law $\xi(t)$ is extracted. Alternatively, one may also determine $\xi(t)$ by fitting $C(r, t)$ to an empirical scaling function [34]

$$C(r, t) = A[\tanh(r/\xi(t))]^{2\alpha}.$$

Both methods yield the same results.

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Fig. 2: (Colour on-line) The correlation length $\xi(t)$ is displayed for different disorders and temperatures on a log-log scale. The curves of $\Delta = 1.2$ are shifted for clarity. Dashed lines represent logarithmic fits to eq. (5). For $\Delta = 1.2$, $\psi = 1.05(7)$ and $0.98(9)$ at $T = 0.67$ and 0.33, respectively. For $\Delta = 0.5$, $\psi = 0.69(5)$ and 0.65(6) at $T = 0.67$ and 0.33, respectively. For $\Delta = 1.5$, $\psi = 1.28(3)$ at $T = 0.67$. In the inset, the height correlation function $C(r,t)$ of $\Delta = 1.2$ and $T = 0.67$ at different times are displayed with solid lines. Symbols show the data collapse according to eq. (13).

Fig. 3: (Colour on-line) The roughness function $\omega^2(t)$ is plotted against $\xi(t)$ on a log-log scale.

The exponents are close to those of the QEW equation. For weak disorder, i.e., $\Delta = 0.5$ and 0.7, and strong disorder, i.e., $\Delta = 1.5$, however, the exponents are obviously different, indicating the dependence of the universality class on the strength of the disorder. Especially, the exponent $\mu$ for the weak disorder is between the random-bond universality class $\mu = 1/4$ and the random-field universality class $\mu = 1$ predicted by the QEW equation. This may give hints for understanding the experiments which yield a similar exponent $\mu$ [25–28]. For the strong disorder, however, the exponent $\mu$ is larger than 1, suggesting a new scenario of the domain-wall motion. On the other hand, although the exponents for the weak disorder depart from those of the QEW equation, the scaling laws in eqs. (3) and (4) always hold within statistical errors, i.e., $\psi \approx \theta$ and $\mu \approx \psi / (2 - \zeta)$. For the strong disorder, the scaling law in eq. (4) is still valid, i.e., $\psi \approx \theta$. However, the scaling law in eq. (3) is obviously violated. This is consistent with the result reported in ref. [29].

Why do the exponents depend on the strength of the disorder? At zero temperature, for $\Delta < 1$, the depinning phase transition is of first order, and the transition field $H_c = \Delta$, since no overhangs can be created, while for $\Delta > 1$, the depinning phase transition is of second order, and the transition field $H_c < \Delta$, since overhangs can be generated [11,18,19,41]. For the creep motion at nonzero temperatures, the driving field $H$ is much smaller than $\Delta$ and $H_c$, and the thermal activation plays an important role in driving the domain wall to propagate. As shown in fig. 4, for the weak disorder, i.e., $\Delta < 1$, overhangs can hardly be seen at low temperatures. For the moderate disorder, i.e., $\Delta$ around or slightly above 1, only a limited number of overhangs may be created. For the strong disorder, i.e., $\Delta \geq 1.5$, overhangs become rather prominent. In other words, the disorder may induce overhangs, and overhangs may change the degree of the interfacial roughness, and therefore alter the universality class.
Table 1: The exponents for the two-dimensional DRFIM model.

<table>
<thead>
<tr>
<th>Δ</th>
<th>T</th>
<th>μ</th>
<th>ψ</th>
<th>ζ</th>
<th>θ</th>
<th>ψ/(2 − ζ)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0.5</td>
<td>0.7</td>
<td>1.0</td>
<td>1.2</td>
<td>1.5</td>
<td></td>
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<tr>
<td>Δ=0</td>
<td>0.67</td>
<td>0.67</td>
<td>0.67</td>
<td>0.67</td>
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<td>0.33</td>
<td>0.33</td>
<td>0.33</td>
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<tr>
<td>Δ=0</td>
<td>0.59(4)</td>
<td>0.73(5)</td>
<td>0.90(5)</td>
<td>0.95(8)</td>
<td>1.44(5)</td>
<td></td>
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<tr>
<td></td>
<td>0.65(6)</td>
<td>0.81(4)</td>
<td>0.94(5)</td>
<td>0.98(9)</td>
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<tr>
<td>Δ=1</td>
<td>0.85(3)</td>
<td>1.01(2)</td>
<td>1.05(7)</td>
<td>1.28(3)</td>
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<tr>
<td></td>
<td>0.81(4)</td>
<td>1.04(5)</td>
<td>1.09(9)</td>
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<tr>
<td>Δ=1</td>
<td>0.98(3)</td>
<td>1.03(3)</td>
<td>1.15(3)</td>
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<td></td>
<td>0.96(6)</td>
<td>1.06(6)</td>
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<td>Δ=1</td>
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<td></td>
<td>0.93(7)</td>
<td>1.10(9)</td>
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<tr>
<td>Δ=1</td>
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<td>1.08(8)</td>
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<td></td>
<td>0.74(5)</td>
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<tr>
<td>Δ=1</td>
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<td>Δ=1</td>
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Fig. 4: The snapshot of the zero-field relaxation process of a domain wall for different disorders at $T = 0.67$ and $t = 10^6$.

However, the overhang might be not the only mechanism which leads to the dependence of the universality class on the strength of the disorder. In fact, the exponents also vary with $\Delta$ in the weak-disorder regime. It may be accidental that the QEW equation describes the creep motion of the domain wall for $\Delta$ around or slightly above 1 [18,38].

In the small-$\zeta(t)$ regime, the roughness exponent is apparently smaller than that in the large-$\zeta(t)$ regime, for example, $\zeta = 0.65(3)$ for $\Delta = 0.5$, which is close to $\zeta = 2/3$ of the random-bond disorder [42,43]. Interestingly, as shown in fig. 3, the curves of different temperatures with the same strength of the disorder collapse onto a single curve, which implies that the temperature only affects the growth law of the correlation length $\xi(t)$. This suggests that there may exist a temperature-independent characteristic length $L_c$ in the dynamic relaxation process. When the correlation length $\xi(t)$ is smaller than $L_c$, $\xi(t)$ grows by a power law and the roughness exponent $\zeta = 0.65(3)$, which may be comparable with the random-bond universality. When the correlation length $\xi(t)$ is larger than $L_c$, the growth law of $\xi(t)$ crosses over to a logarithmic one.

**Conclusion.** – To summarize, we have simulated the creep motion of a domain wall in the two-dimensional random-field Ising model with a driving field. The nonlinear field-velocity relation in eq. (1) is confirmed, and the creep exponent $\mu$ is determined. Meanwhile, we also measure the roughness exponent $\zeta$ and energy barrier exponent $\psi$ from the zero-field relaxation process. For the moderate disorder, i.e., $\Delta$ around or slightly above 1, all the exponents are close to those predicted by the Edwards-Wilkinson equation; for the weak and strong disorder, however, the exponents are very much different, showing dependence on the strength of the disorder. For the weak and moderate disorder, the scaling laws in eqs. (3) and (4) always hold. For the strong disorder, the scaling law in eq. (3) is violated.

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